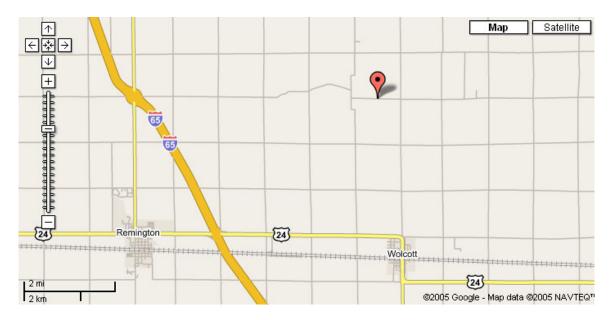
Homework 5. CE506 Fall, 2005 Position Estimation with GPS Pseudoranges

Assigned Thursday 20 October, Due Thursday 27 October

Get the data file GPS.dat which has been extracted from a RINEX (receiver independent exchange) format file for a nearby CORS (continuously operating reference station) station, WLCI north of Wolcott, Indiana. See regional map. The data was acquired on 19 December, 2004 beginning at 1:00am GMT (that's 18 December 8:00pm Indiana time). We want to estimate the receiver location (XYZ) from the observed pseudoranges. Note that all coordinates are in an *earth fixed* coordinate system.



See also the file sample_code1.m which gives some hints and template code, and suggests a structure or framework for your program. Make sure you remove all of the header information and annotation before you try to read the data with "textread". It will complain if there is anything other than numbers in columns.

- 1. Use ONLY the P1 pseudorange (ignore the second one, P2), refined by the dt value in column 8. Use ONLY data for epoch 0 (6 observations). Assume equal precision for observations. Use given values in the header data for initial approximations of the 3 unknown receiver coordinates, use zero as initial approximation of the receiver clock bias unknown.
- 2. Use ONLY the P1 pseudorange as in problem 1, but now include all observations for all 6 epochs. You should have 3 coordinate unknowns and 6 receiver clock bias unknowns, total = 9.

```
$ -----
 Observation and orbit data extracted from wlci3540.04o and igr13020.sp3
   Approximate receiver position : 248645.5722 -4828261.0758 4146460.5047
   Epoch for the first observation: 2004 12 19 1 0 0.0000000
          : epoch (each epoch is 15 min apart in this file)
   P1 & P1 : pseudoranges (m)
           : satellite id
   Xs, Ys, Zs: satellite orbits (km)
           : correction for satellite clock error (*1e-6 sec)
   ** pseudorange(corrected) = pseudorange(original) + C*dt
                                                                      C: speed of light
  ** a receiver clock offset needs to be estimated for each epoch
 This file is prepared by Geomatics Enq. Purdue Univ. Oct. 5, 2005
 ______
           P1
                            P2
                                        SV
                                                                Ys
 epoch
                                                 Xs
                                                                                Zs
                                                                                                 dt.
     22496829.2274
                                             -17319.788298 -18753.615405
                                                                            7289.870513
                        22496831.7114
                                        30
                                                                                             480.699220
   0
                                             -13620.412090 -8139.476238 21491.132873

8090.235212 -23994.024327 -7525.939414

19299.426506 -9601.408628 15858.224435

23451.225526 -6720.739536 10909.611230
      22324959.7344
23706277.0944
   0
                        22324962.8874
                                        6
                                                                                             440.629976
                        23706281.6764
                                        29
   0
                                                                                             228.388663
                        22845705.6804
       22845702.0944
                                        24
                                                                                              81.677538
   0
                                                                                             497.205031
       24096681.1564
                        24096682.7854
                                        4
   0
                        20924321.2664
                                              11658.840158 -13418.617818 19408.086808
       20924321.1484
                                         2
                                                                                             -61.530143
   0
                                             -17457.515309 -19506.125796
                        23062177.7814
       23062175.3674
                                        3.0
                                                                             4587.087502
                                                                                             480.688424
   1
                                             -12467.177318 -10262.683615 21268.893874
8615.173659 -24545.007367 -4737.107771
                        22080312.7774
       22080309.6024
                                        6
                                                                                             440.613252
   1
      23322425.5864
                        23322429.0434
                                        29
                                                                                             228.373546
                                              20937.852145 -9378.991848 13744.183809
24543.262918 -6496.455396 8374.871353
       23435240.0164
                        23435245.0784
                                                                                              81.680274
   1
                                        2.4
   1
       24770290.3364
                        24770293.7234
                                                                                             497.187590
                                             13861.686454 -13302.740503 18004.091678
-12533.818460 -22979.450692 -5167.650272
-17451.847231 -19998.356157 1805.470225
       21415132.5004
                        21415132.3364
   1
                                                                                             -61.521529
   1
       24258337.6954
                        24258341.6684
                                                                                              66.468047
       23687642.5754
                        23687645.0244
                                       3.0
                                                                                             480.677596
                                             -11436.242495 -12399.620747 20686.561314
       21890970.9504
                        21890973.9034
                                         6
                                                                                             440.596661
                                              8971.718933 -24830.803485 -1865.612226
22336.818843 -9238.262709 11398.461343
       22969209.1614
                        22969212.6534
                                        29
                                                                                             228.358428
       24040953.4744
                        24040958.3254
                                        24
                                                                                              81.682668
       21947855.4194
                        21947855.5484
                                              15887.709170 -13286.773786 16282.090524
                                                                                             -61.512942
                                             -11849.062368 -22600.178999 -7831.385776
       24993027.2944
                        24993032.8494
                                                                                             66.469970
                                             -17270.599926 -20245.980592 -1007.095561
-10539.285165 -14506.123591 19753.515071
   3
       24357629.5414
                        24357632.0844
                                        3.0
                                                                                             480.666741
   3
       21768498.8464
                        21768501.8224
                                                                                             440.579903
                                         6
                                                                           1038.357441
                                              9191.986463 -24828.935055
23469.237047 -9147.384289
   3
       22662260.5494
                        22662263.0214
                                        29
                                                                                             228.343814
                                        24
   3
       24662263.2994
                        24662267.9044
                                                                             8860.171168
                                                                                              81.684425
       22520313.8614
                        22520313.6624
                                              17698.794668 -13345.581266 14272.983399
                                                                                             -61.504291
   3
       25724907.7604
                        25724913.0804
                                         5
                                             -10952.259109 -22038.392415 -10362.334919
                                                                                              66.472456
                                             6882.513196 -25086.995312 -3664.922302
-22230.159999 -6638.521293 13312.449879
       23215756.7914
                        23215759.2754 26
                                                                            -3664.922302
                                                                                             299.590732
       24919871.2364
                        24919872.4084
                                        21
                                                                                             85.166637
   3
                                              8244.527292 -14724.499137
       21404066.8934
                        21404070.9244
                                        17
                                                                            20552.901880
                                                                                            -134.728636
                                               5790.833476 -15144.585608
       21040817.2054
                        21040820.8614
                                        10
                                                                            20917.835004
                                                                                              55.675143
       24456705.2734
                        24456707.8284
                                             -16886.333963 -20271.742779
                                                                            -3802.488153
                                                                                             480.655756
                                        30
                        21124237.0864
                                              -9780.423908 -16537.212230 18485.028420
       21124234.2274
                                         6
                                                                                             440.563446
                                              9312.341481 -24525.286592
24315.576292 -9070.781765
                        21817207.2704
                                                                            3924.353411
       21817204.5864
                                                                                             228.328703
       24699396.4844
                        24699397.8674
                                                                             6171.814344
                                                                                              81.686640
       22530998.9614
                        22531000.4844
                                              19263.607865 -13448.563772 12012.726046
                                                                                             -61.495938
       22197946.5234
                        22197949.3954
                                        26
                                               7172.813851 -25223.013411
                                                                             -740.487959
                                                                                             299.597240
       24027129.6484
                        24027129.8484
                                        21
                                             -20651.120555 -7089.730250 15412.727810
                                                                                              85.167407
       25168125.9354
                        25168130.0604
                                             -16277.524136 -20104.409411
                                                                            -6533.158122
                                                                                             480.645091
       21166414.7004
                        21166417.8294
                                         6
                                             -9156.165921 -18448.642493 16902.058120
                                                                                             440.547000
                                               9371.760136 -23914.666296
       21646802.3804
                        21646805.4034
                                        29
                                                                             6742.569093
                                                                                             228.313956
                                              24864.538769 -8970.633770
       25351062.3104
                        25351064.7824
                                        24
                                                                             3378.630975
                                                                                              81.690339
       25091313.6534
                        25091316.9354 18
                                             -19808.555621 -17782.224154 -2007.117328
                                                                                            -108.464373
                        23176824.0834
                                             20558.638891 -13561.025469 9541.613930
       23176823.5214
                                                                                             -61.487195
                       21837405.2354 26
                                               7368.212459 -25048.401371
                                                                            2197.138121
       21837402.8564
                                                                                             299.603583
```

```
sample_code1.m
% note: this sample code can be used as a template, to be expanded to work
% with the real gps pseudorange equations
% it does NOT do anything useful if you run it as is !
% you may experiment with the symbolic matlab tools as shown here
% or you may do the old fashioned way with analytically derived expressions
% but let the program construct elements the J-matrix and the f-vector
% and fill them in automatically
% note least wquares code is for a 2D range problem with no clock unknowns
% you have to make MANY changes for homework 5.
clc; % clear screen
clear all; % Removes all variables, functions, and MEX-files from memory, leaving the workspace empty.
close all; % deletes all figures whose handles are not hidden
format long; % Scaled fixed-point format with 15 digits
format compact % don't waste so much paper
datestr (now)
[\texttt{epoch\_n,pr1,pr2,sat\_n,sat\_x,sat\_y,sat\_z,sat\_t}] = \texttt{textread('GPS.dat', '%d %f %f %f %f %f %f )';} \\
% Intitial Estimation for x, y, z (location of receiver) and % dtt is receiver clock offset (error)
8 -----
x = 200000; % meters
y = -4000000; % meters z = 4000000; % meters
dtt = zeros(6,1); % receiver time offset
c = 299792458; % speed of light; unit: meters per second
% how to use sym function and diff or jacobian function here?
% the following equations are just for demo, not the correct ones for our homework
Fi = sym('sqrt((sx-x)^2+(sy-y)^2)');
% for differentiating, you select either
$ ______
dFdU = jacobian(Fi,[sym('x') sym('y')]);
dFdx = diff(Fi,'x');
dFdy = diff(Fi, 'y');
L = pr1(1:6); % use pr1 for range observations
W = diag(ones(1,6)); % weight matrix
\max \det a = 1; % Initial Value for maximum absolute value of delta x, delta y, and delta z iter = 0; % Iteration Count
while max delta>1e-9
       fprintf('\n----\n');
       iter = iter + 1;
       F = zeros(6,1);
       J = zeros(6,2);
       for i = 1:6
              sx = sat_x(i);
              sy = sat_y(i);
              F(i) = eval(Fi);
              J(i,:) = eval(dFdU); % or <math>JJ(i,:) = [eval(dFdx) eval(dFdy)];
       end
       f = L-F;
delta = inv(J'*W*J)*J'*W*f
       x = x + delta(1)
       y = y + delta(2)
       max_delta = max(abs(delta));
       break:
end
v = J*delta-f
L hat = L+v
```