

1. Given 4 points in the XY plane:

$(1.0, 2.7684)$, $(2.0, 2.5461)$, $(3.0, 2.076)$, $(-3.3, 1.3682)$ which lie on the ellipse:

$$\boxed{\frac{(x-x_0)^2}{a^2} + \frac{(y-y_0)^2}{b^2} = 1}$$
, find the ellipse parameters $x_0, y_0,$

$a,$ and b by Newton iterations. You may find another method to solve this problem (determinant formula, etc.) which is OK for check, but do not use "exact parameter values" as your initial approximations. (We need to see convergence)

2. An air vehicle makes 2 passes by a point of interest. The first pass starts at $t=0s$ at location $(10000, 5000, 1000)m$, with velocity:

$$\vec{V}_1 = \begin{bmatrix} 9.315322 \\ 52.829815 \\ 0 \end{bmatrix} \text{ m/s}$$

The second pass starts at $t=500s$ at location $(11865.808, 6550.165, 1000)m$

with velocity: $\vec{V}_2 = \begin{bmatrix} 9.315322 \\ -52.829815 \\ 0 \end{bmatrix} \text{ m/s}$. 3D range observations

to the point of interest on the ground ($z < 200m$) are made at the following times:

$t(s)$	$d(m)$	
0	1721.09	} first pass
10	1448.17	
20	1345.76	
30	1447.97	
40	1720.89	
500	1318.05	} second pass
510	1204.46	
520	1317.85	

The ground point is to the right of both trajectories. Positions and velocities of vehicle are known exactly. Use indirect observations to find the coordinates of the unknown point. All observations have equal weights. Why does first trajectory only fail?