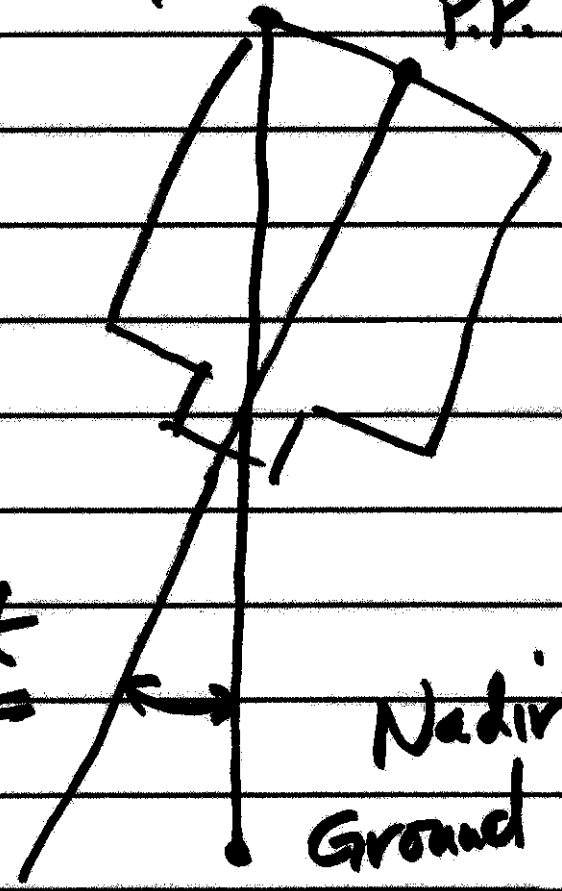
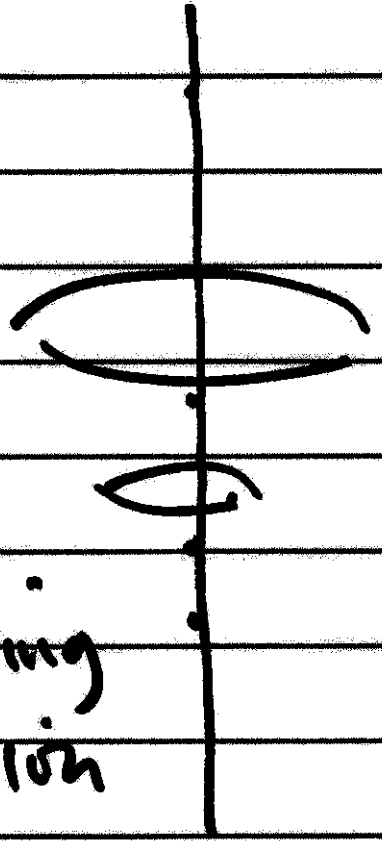
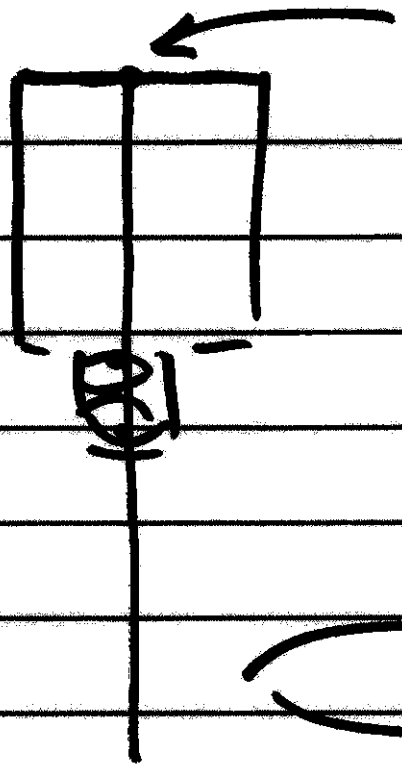


Principal point

Nadir

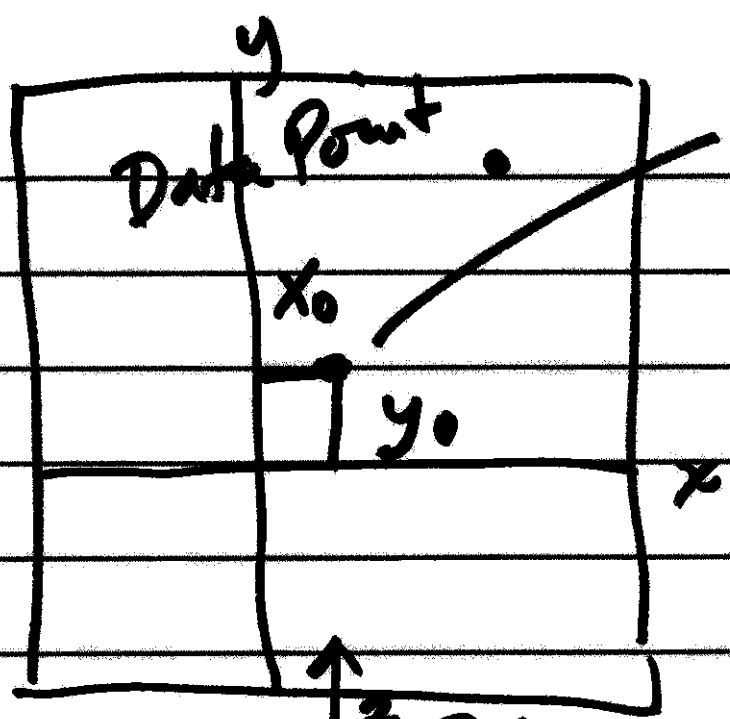
P.P.



decentering distortion

tilt

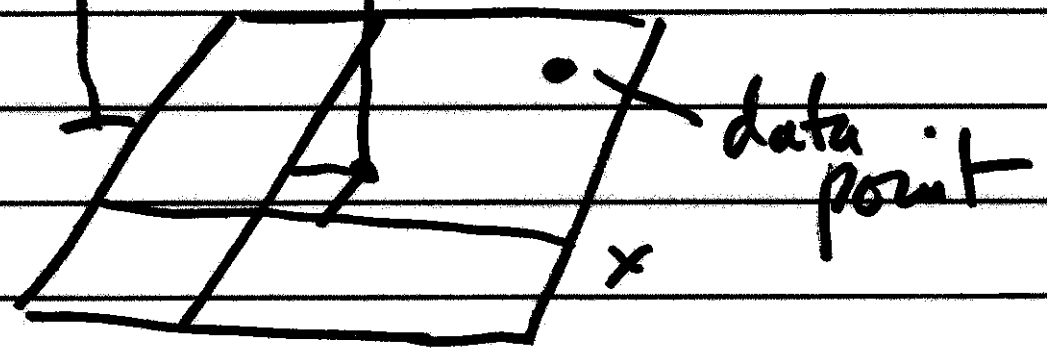
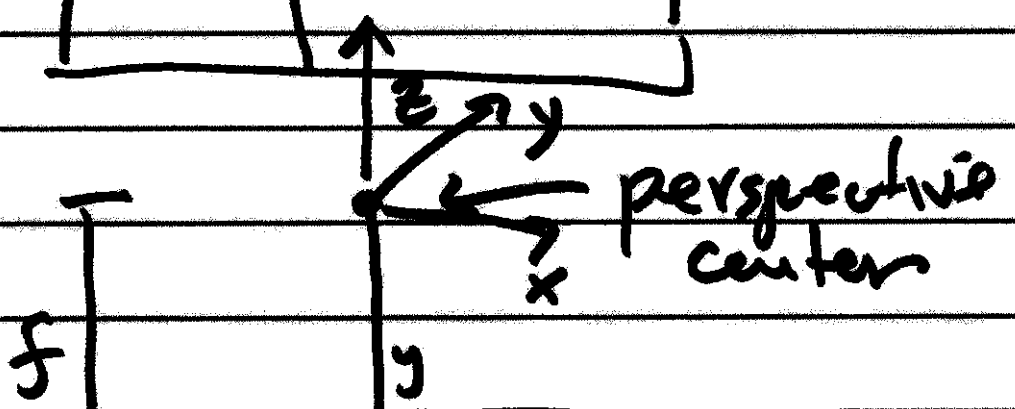
Nadir  
Ground



Princ. Point

$(x - x_0, y - y_0)$  2D  
 image coordinates

$\begin{pmatrix} x - x_0 \\ y - y_0 \\ -f \end{pmatrix}$  3D  
 sensor coord.



$$\begin{pmatrix} x \\ y \\ z_0 \end{pmatrix} = \begin{pmatrix} x' \\ y' \\ w \end{pmatrix}$$

$$x = \frac{x'}{w}$$

$$y = \frac{y'}{w}$$

Homogeneous  
Coordinates

$$\begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix}$$

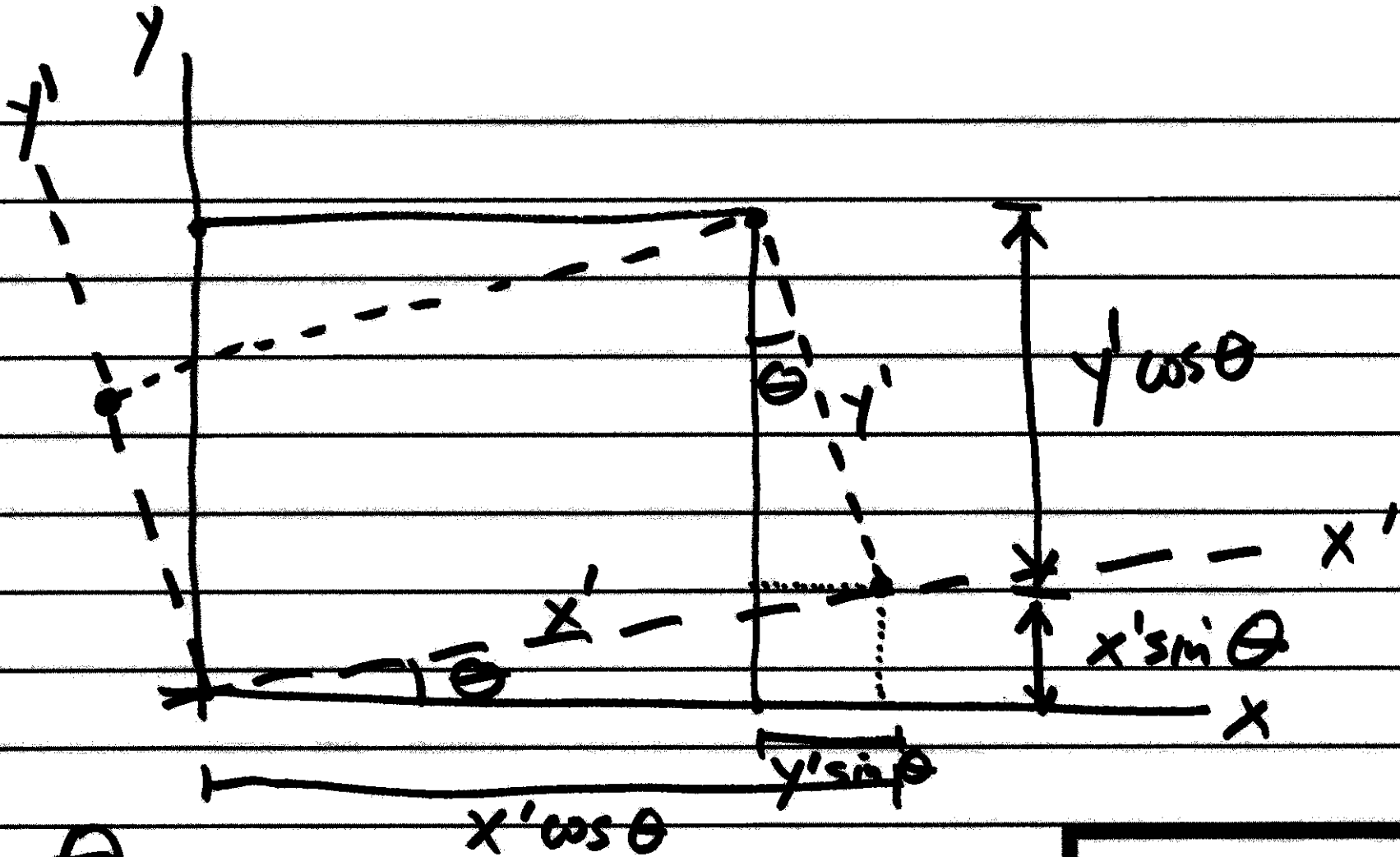
$$x'_T = x' + t_x w$$

$$y'_T = y' + t_y w$$

⋮

$$\begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix}_{\text{Rot}} = \begin{bmatrix} M_{3 \times 3} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix}$$

$$\begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix}_{\text{Scaled}} = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x' \\ y' \\ z' \\ w \end{pmatrix}$$


 $\theta$ 

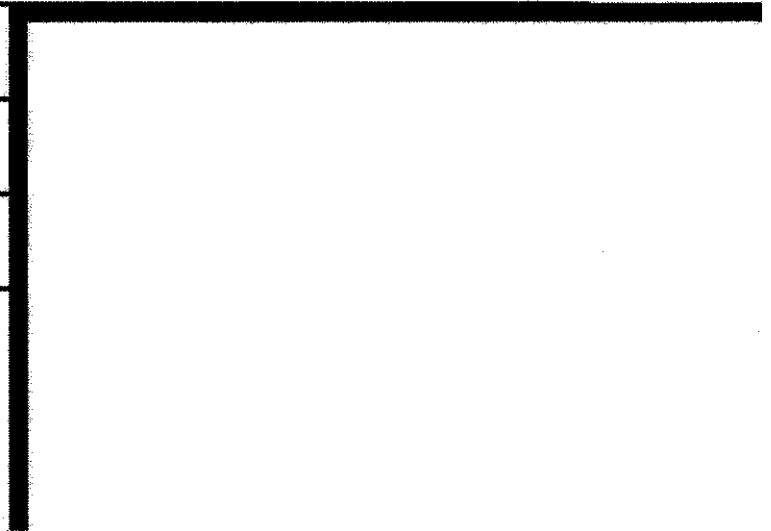
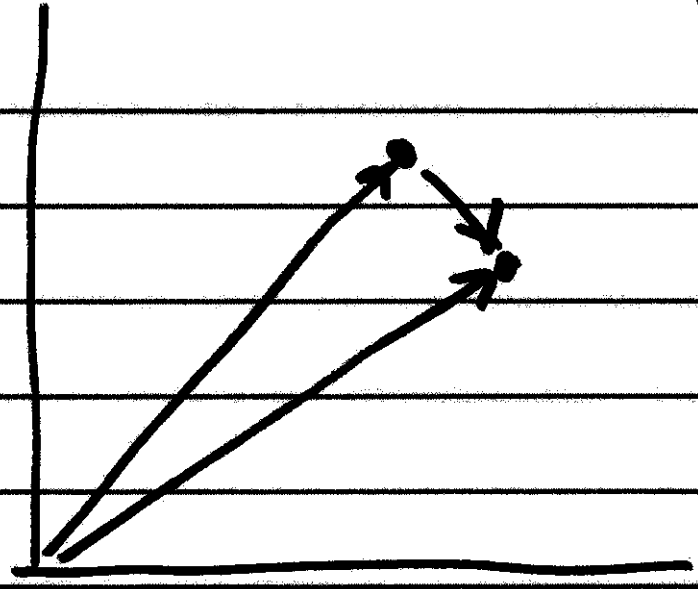
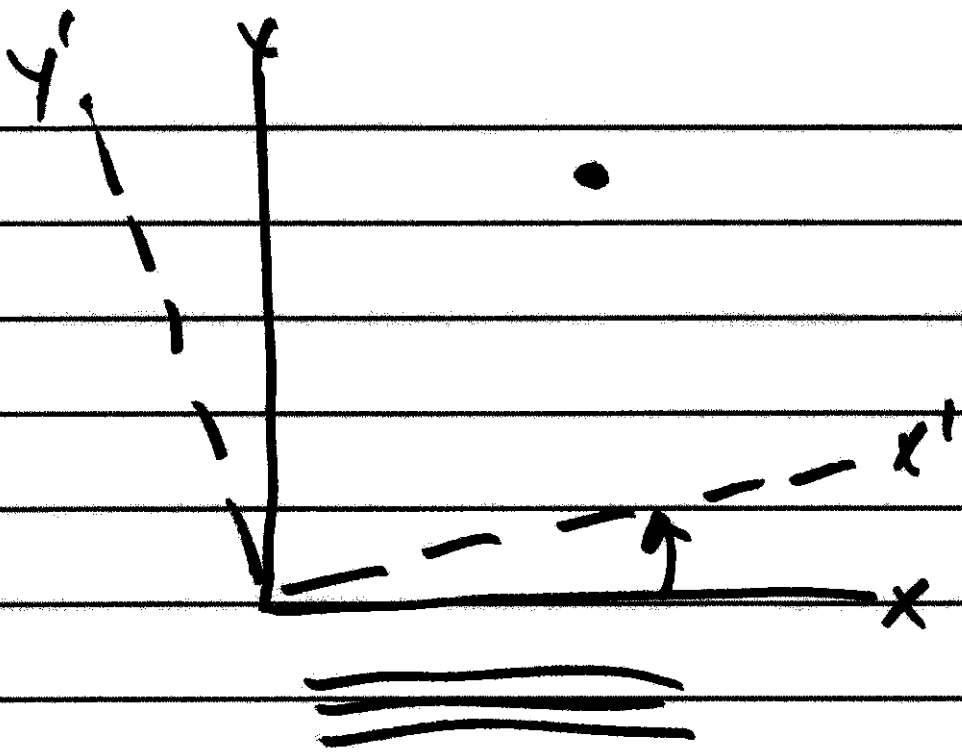
$$x = x' \cos \theta - y' \sin \theta$$

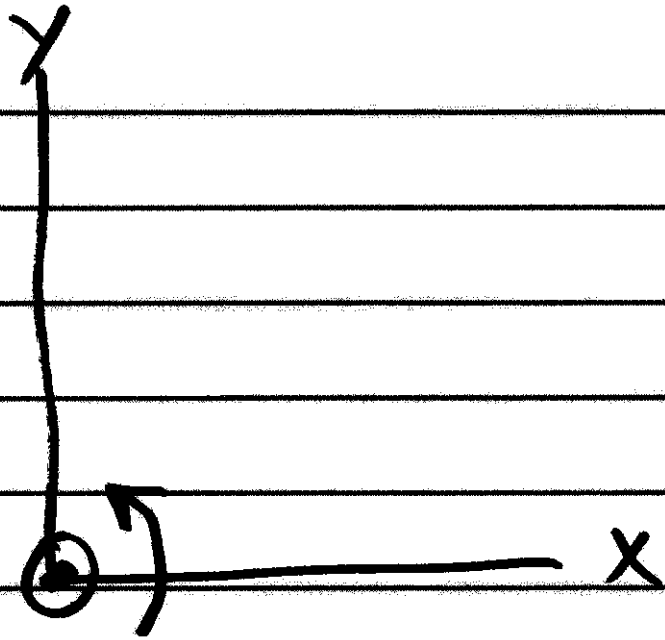
$$y = x' \sin \theta + y' \cos \theta$$

$$\begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} x' \\ y' \end{pmatrix}$$

matrix orthogonal  
inverse = transpose

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$





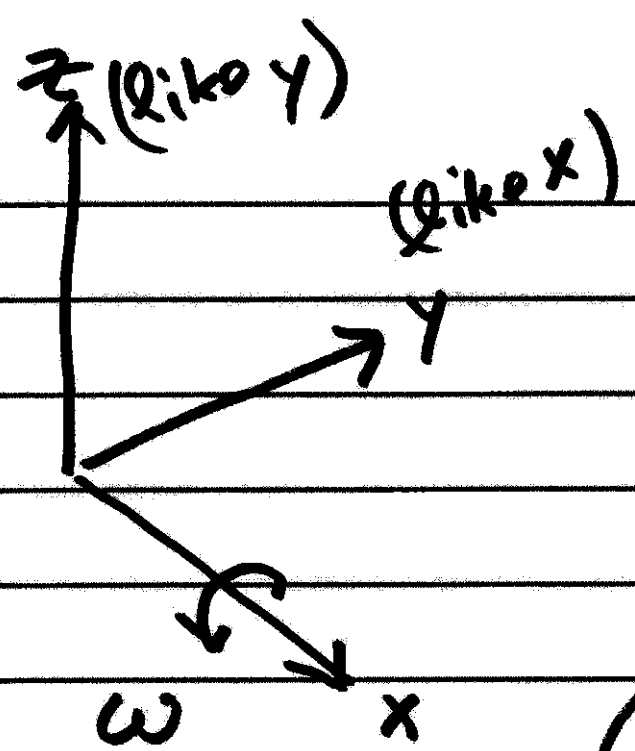
$\kappa$  : Kappa

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} \cos \kappa & \sin \kappa & 0 \\ -\sin \kappa & \cos \kappa & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} \quad \text{5-8}$$

$M_{\kappa}$

$R_3$





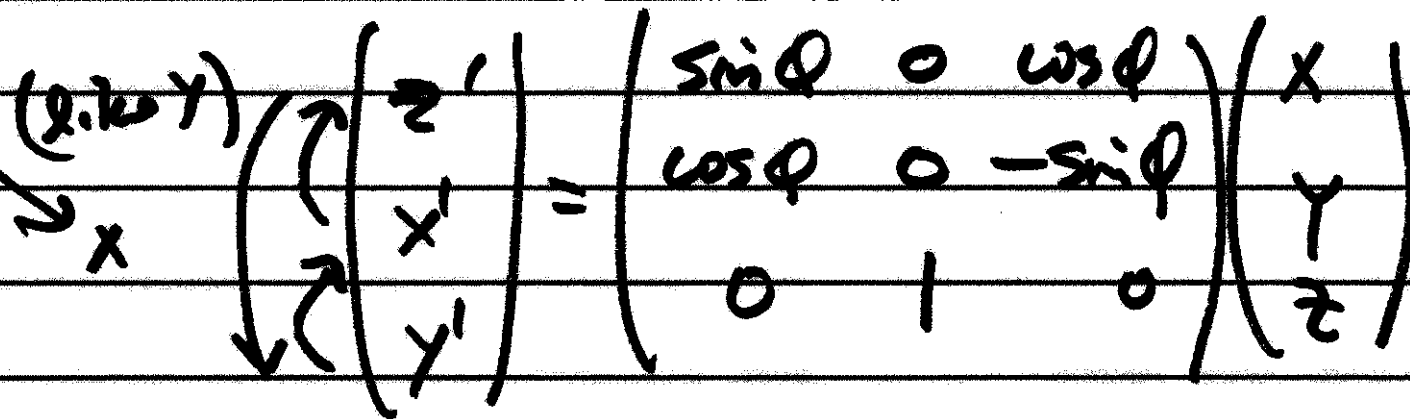
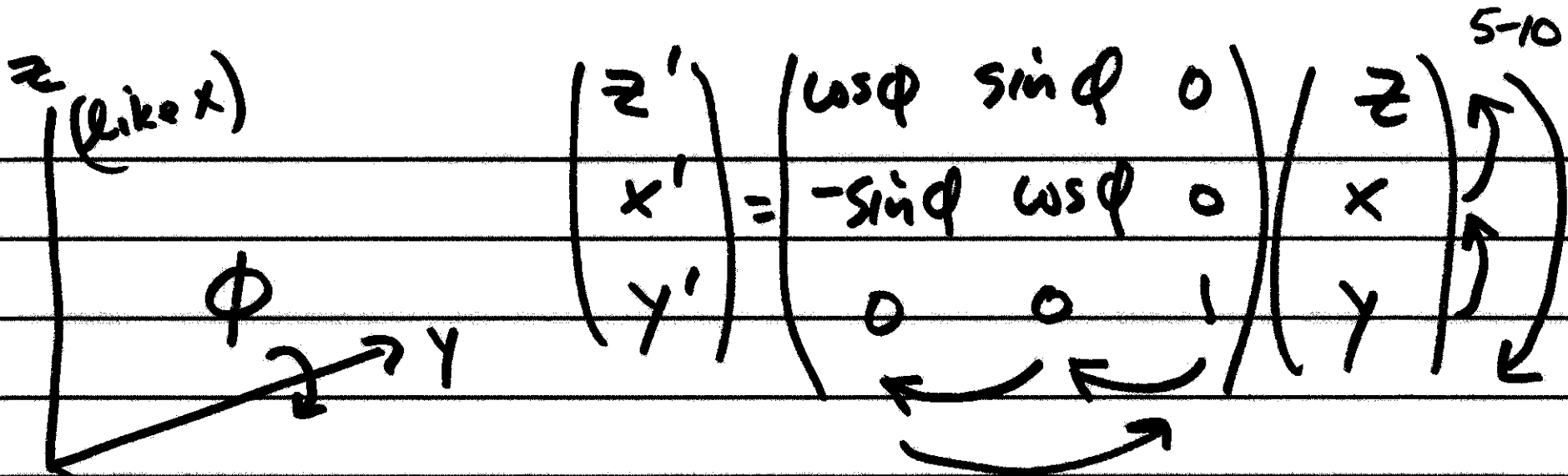
$$\begin{pmatrix} y' \\ z' \\ x' \end{pmatrix} = \begin{pmatrix} \cos \omega & \sin \omega & 0 \\ -\sin \omega & \cos \omega & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} y \\ z \\ x \end{pmatrix}$$

$\ominus_x$   
 $\ominus_z$

$$\begin{pmatrix} y' \\ z' \\ x' \end{pmatrix} = \begin{pmatrix} 0 & \cos \omega & \sin \omega \\ 0 & -\sin \omega & \cos \omega \\ 1 & 0 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \omega & \sin \omega \\ 0 & -\sin \omega & \cos \omega \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

$M_x, R_1$



$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} \cos\phi & 0 & -\sin\phi \\ 0 & 1 & 0 \\ \sin\phi & 0 & \cos\phi \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

$M_\phi, R_2$

$$M = \begin{bmatrix} \cos\phi \cos\kappa & \cos\omega \sin\kappa + \sin\omega \sin\phi \cos\kappa \\ -\cos\phi \sin\kappa & \cos\omega \cos\kappa - \sin\omega \sin\phi \sin\kappa \\ \sin\phi & -\sin\omega \cos\phi \end{bmatrix}$$

↓

3x3

$$\left. \begin{array}{l} \sin\omega \sin\kappa - \cos\omega \sin\phi \cos\kappa \\ \sin\omega \cos\kappa + \cos\omega \sin\phi \sin\kappa \\ \cos\omega \cos\phi \end{array} \right\}$$

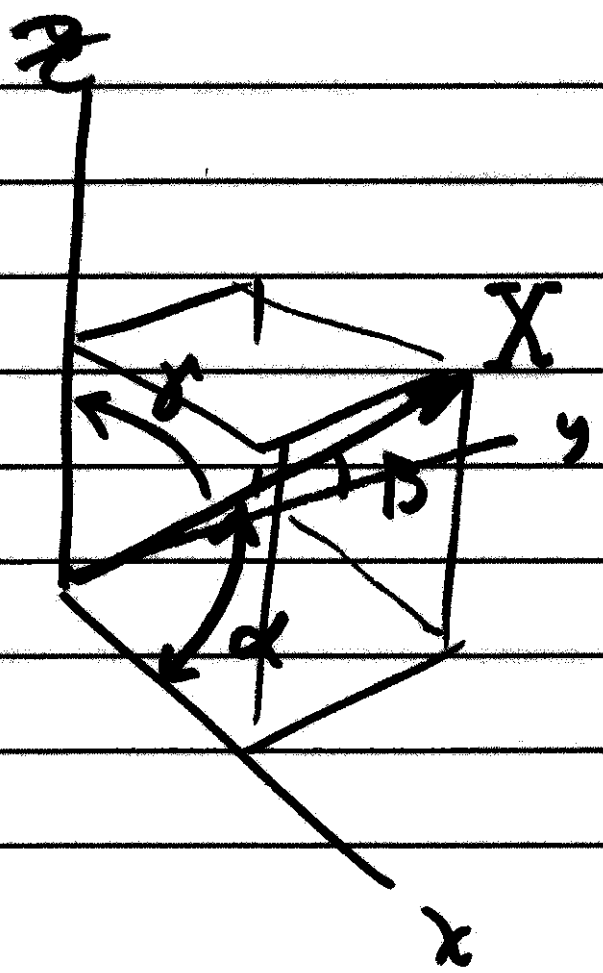
$$\underline{M = M_K M_\phi M_\omega}$$

$$M = \underbrace{M_K M_\varphi M_\omega}_{\leftarrow}$$

$$M = M_\varphi M_\omega M_K$$

$$M = M_K M_\omega M_K$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = M \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \quad M = \begin{pmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{pmatrix}$$



$$\begin{pmatrix} M_{11} \\ M_{21} \\ M_{31} \end{pmatrix} = M \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \quad \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \quad \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} \cos \alpha \\ \cos \beta \\ \cos \gamma \end{pmatrix}$$

$$M = \begin{bmatrix} \cos x X & \cos x Y & \cos x Z \\ \cos y X & \cos y Y & \cos y Z \\ \cos z X & \cos z Y & \cos z Z \end{bmatrix}$$

direction cosines

# algebraic parameters

5-15

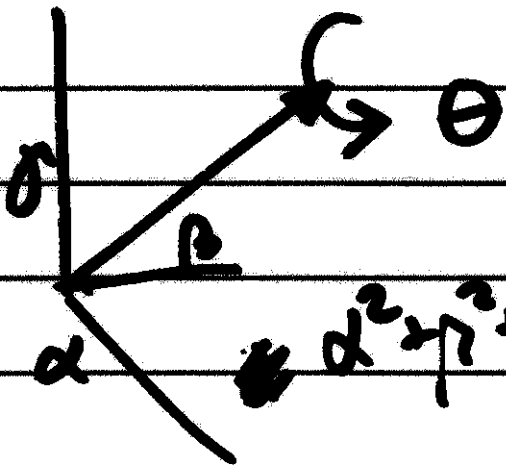
$$M = \begin{bmatrix} d^2 + a^2 - b^2 - c^2 & 2(ab + cd) & 2(ac - bd) \\ 2(ab - cd) & d^2 - a^2 + b^2 - c^2 & 2(bc + ad) \\ 2(ac + bd) & 2(bc - ad) & d^2 - a^2 - b^2 + c^2 \end{bmatrix}$$

$$a^2 + b^2 + c^2 + d^2 = 1$$

## Rotation @ directed line

$$M = \begin{bmatrix} \alpha^2(1-\cos\theta) + \cos\theta & \alpha\beta(1-\cos\theta) - j\sin\theta \\ \alpha\beta(1-\cos\theta) + j\sin\theta & \beta^2(1-\cos\theta) + \cos\theta \\ \alpha\gamma(1-\cos\theta) - \beta\sin\theta & \beta\gamma(1-\cos\theta) + \alpha\sin\theta \end{bmatrix} \quad \downarrow$$

$$\begin{bmatrix} \alpha\gamma(1-\cos\theta) + \beta\sin\theta \\ \beta\gamma(1-\cos\theta) - \alpha\sin\theta \\ \gamma^2(1-\cos\theta) + \cos\theta \end{bmatrix}$$



$$\alpha^2 + \beta^2 + \gamma^2 = 1$$