Image Coordinate Refinement & Camera Calibration

Measurement system (row,column) defined with respect to digital image

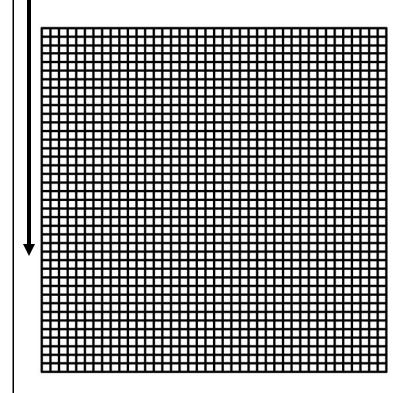
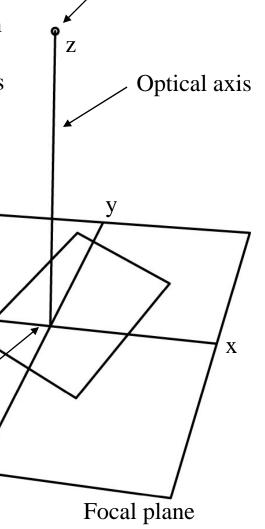


Image (2D) and sensor (3D) coordinate system defined with respect to focal plane, optical axis and reference direction



Perspective center

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Principal point

Coordinate Transformations to relate measurement (r,c) and image (x,y) coordinate systems

Write equations at fiducial marks or reseau marks or any other fixed points which are known or observed in *both* systems. Solve for parameters with those equations – then apply at all other measured points.

4 - parameter, nonlinear

$$\begin{bmatrix} r \\ c \end{bmatrix} = \lambda \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

4 - parameter, linear

$$\begin{bmatrix} r \\ c \end{bmatrix} = \begin{bmatrix} a & b \\ -b & a \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} c \\ d \end{bmatrix}$$

6 - parameter, affine, nonlinear

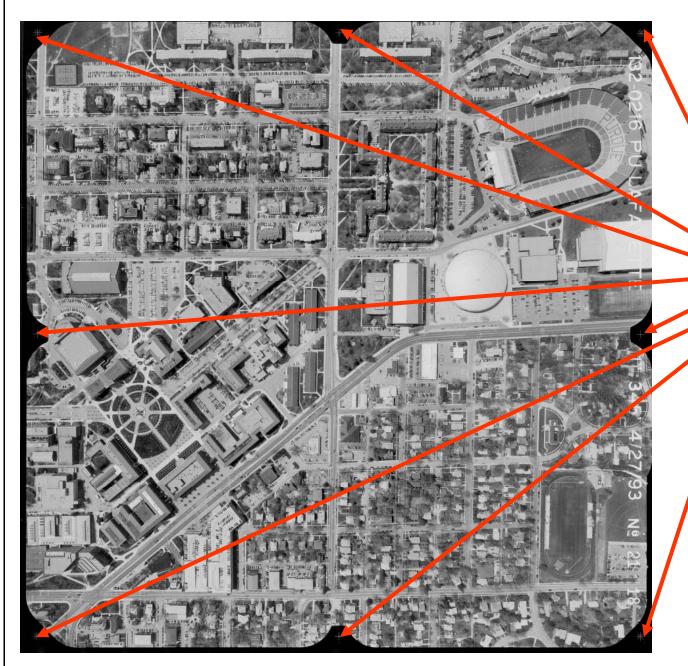
$$\begin{bmatrix} r \\ c \end{bmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} 1 & 0 \\ \alpha & 1 \end{bmatrix} \begin{bmatrix} S_x & 0 \\ 0 & S_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

6 - parameter, affine, linear

$$\begin{bmatrix} r \\ c \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ x \end{bmatrix} + \begin{bmatrix} e \\ f \end{bmatrix}$$

8 - parameter, nonlinear

$$r = \frac{a_1 x + b_1 y + c_1}{a_0 x + b_0 y + 1}$$
$$c = \frac{a_2 x + b_2 y + c_2}{a_0 x + b_0 y + 1}$$



Fiducial marks – given in camera calibration report

Lens Distortion (radial)

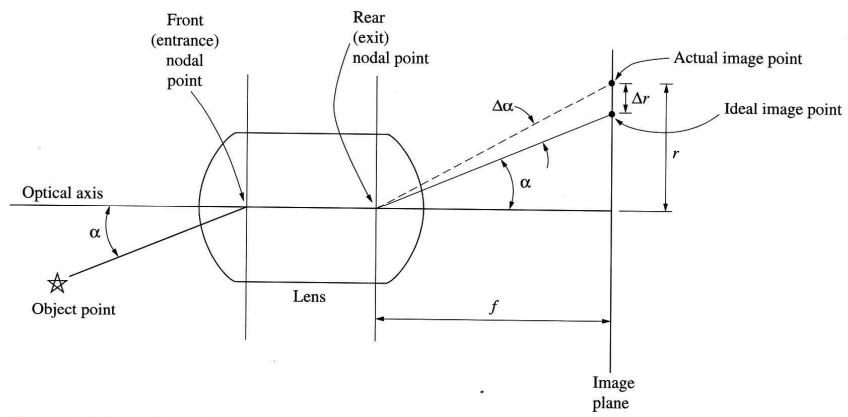


Figure 4-7 Lens distortion.

$$\Delta r = k_0 r + k_1 r^3 + k_2 r^5 + k_3 r^7$$

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Decentering Distortion

$$x' = x - x_0$$

$$y' = y - y_0$$

$$r = \sqrt{(x')^2 + (y')^2}$$

$$dx_d = P_1(r^2 + 2(x')^2) + 2P_2x'y'$$

$$dy_d = P_2(r^2 + 2(y')^2) + 2P_1x'y'$$

Exaggerated effects of radial lens distortion

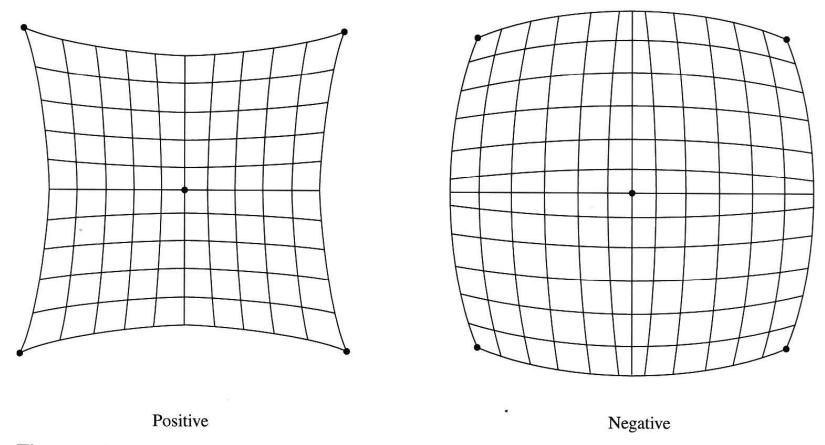


Figure 3-7 Positive and negative radial distortion.

Laboratory calibration instrument to project targets at fixed angles into the camera (multi-collimator, USGS laboratory)

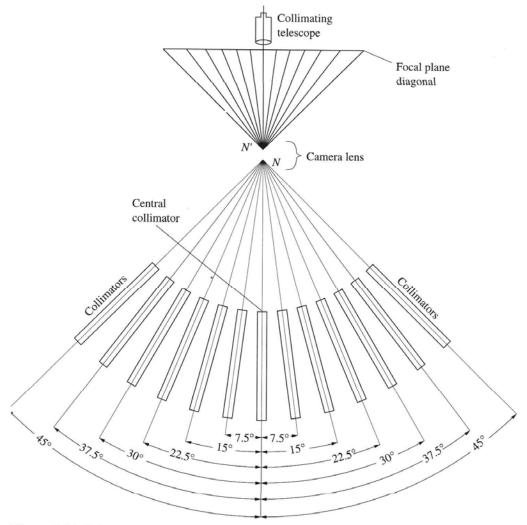
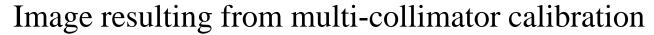
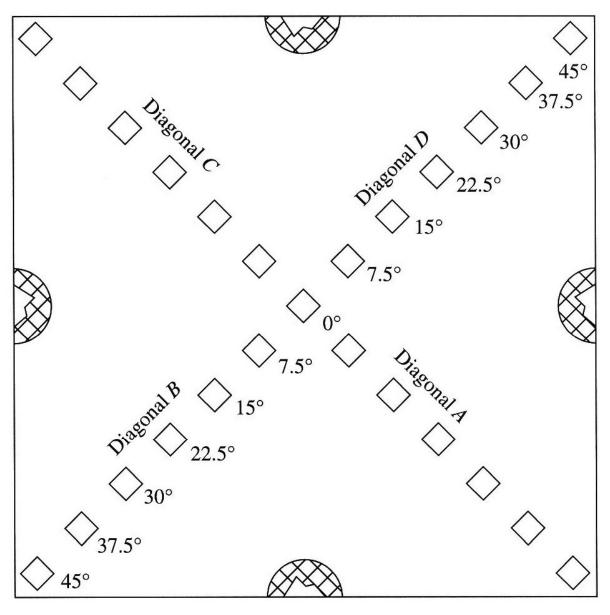


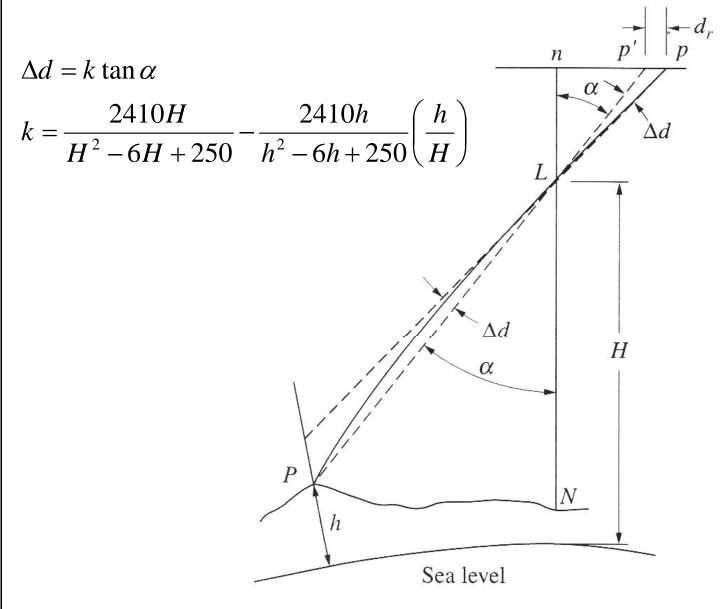
Figure 3-31 Schematic of a multicollimator for mapping camera calibration.



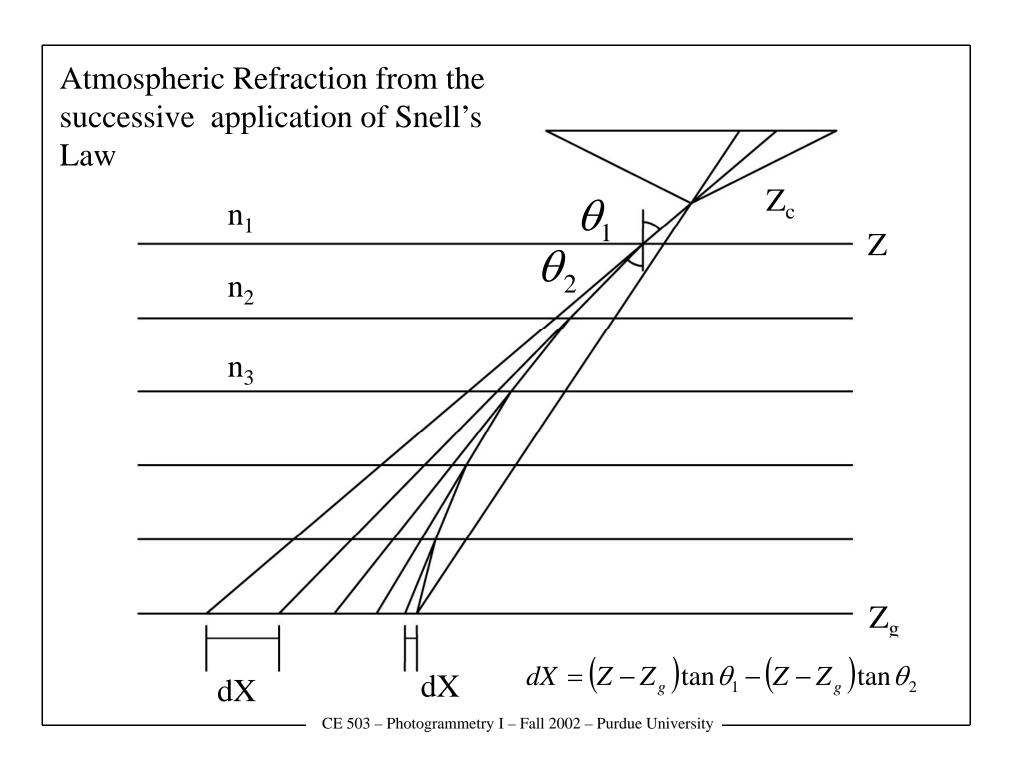








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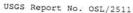






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Prepared under sponsorship of
ENVIRONMENTAL SCIENCE SERVICES ADMINISTRATION
NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
UNITED STATES AIR FORCE





United States Department of the Interior

U.S. GEOLOGICAL SURVEY Reston, Virginia 20192

REPORT OF CALIBRATION of Aerial Mapping Camera

December 18, 1998

13055

Camera type: Wild RC10 Lens type:

Wild Universal Aviogon /4

Camera serial no.: 1394 Lens serial no.:

Nominal focal length: 153 mm

Maximum aperture: f/4 Test aperture: f/4

Submitted by: Dickerson Aerial Surveys, Inc.

Lafayette, Indiana

Reference:

Letter dated December 14, 1998, from Mr. John D. Dickerson.

These measurements were made on Kodak Micro-flat glass plates, 0.25 inch thick, with spectroscopic emulsion type 157-01 Panchromatic, developed in D-19 at 68° F for 3 minutes with continuous agitation. These photographic plates were exposed on a multicollimator camera calibrator using a white light source rated at approximately 5200K.

Calibrated Focal Length: 153.077 mm

II. Lens Distortion

Field angle:	7.5°	15°	22.7°	30°	35°	40°
Symmetric radial (um)	-1	-2	-1	0	2	- 1
Decentering (um)	0	0	o	1	1	2

Symmetric radial distortion parameters		Decentering distortion parameters				Calibrated principal point							
K ₀ K ₁ K ₂ K ₃	= =	0.6142 x 1 -0.1179 x 1 0.4519 x 1 0.0000	0-7	P ₁ P ₂ P ₃ P ₄	= = =	-0.1235 0.9974 0.0000 0.0000				×р Ур	=	0.005	
4	=	0.0000		4									

The values and parameters for Calibrated Focal Length (CFL), Symmetric Radial Distortion (K_0,K_1,K_2,K_3,K_4) , Decentering Distortion (P_1,P_2,P_3,P_4) , and Califold brated Principal Point [point of symmetry] $(\mathbf{x}_p, \mathbf{y}_p)$ were determined through a least-squares Simultaneous Multiframe Analytical Calibration (SMAC) adjustment. The x and y-coordinate measurements utilized in the adjustment of the above parameters have a standard deviation (σ) of ± 3 microns.

USGS Report No. OSL/2511

III. Lens Resolving Power in cycles/mm

Area-weighted average resolution: 80

Field angle:	0 °	7.5°	15°	22.7°	30°	35°	40°
Radial Lines	113	113	80	57	95	95	67
Tangential lines	113	113	80	67	80	80	67

The resolving power is obtained by photographing a series of test bars and examining the resultant image with appropriate magnification to find the spatial frequency of the finest pattern in which the bars can be counted with reasonable confidence. - The series of patterns has spatial frequencies from 5 to 268 cycles/mm in a geometric series having a ratio of the 4th root of 2. Radial lines are parallel to a radius from the center of the field, and tangential lines are perpendicular to a radius.

IV. Filter Parallelism

The two surfaces of the Wild No. 7419, the 500 Pan No. 4006, and the 525 No. 7415 filters accompanying this camera are within 10 seconds of being parallel. The 525 filter was used for the calibration.

Shutter Calibration

Indicated exposure time	Effective exposure time	Efficiency
1/200	5.50 ms = 1/180 s	81%
1/400	2.63 ms = 1/380 s	81%
1/600	1.75 ms = 1/570 s	81%
1/800	1.31 ms = 1/760 s	81%
1/1000	1.05 ms = 1/950 s	81%

The effective exposure times were determined with the lens at aperture f/4. The method is considered accurate within 3 percent. The technique used is Method I described in American National Standard PH3.48-1972 (R1978).

VI. Film Platen

The film platen mounted in Wild RC10 drive unit No. 1394-68 does not depart from a true plane by more than 13 um (0.0005 in).

This camera is equipped with a platen identification marker that will register "68" in the data strip area for each exposure.

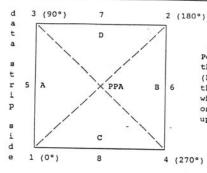
(2 of 4)

Y coordinate

109.988

-110.025

VII. Principal Points and Fiducial Coordinates



Positions of all points are referenced to the principal point of autocollimation (PPA) as origin. The diagram indicates the orientation of the reference points when the camera is viewed from the back, or a contact positive with the emulsion up. The data strip is to the left.

X coordinate

0.004

0.003

Indicated pri	ncipal point, corn ncipal point, mids nt of autocollimat incipal point (pt.	ide fiducials	0.003 mm 0.004 0.0 0.005	-0.001 mm -0.001 0.0 -0.004
	Fiducial Marks			
	1		-106.006 mm	-106.003 mm
	2		106.003	105.993
	3		-105.991	105.999
	5		105.998	-106.003
	6		-110.002	-0.002
			110.042	-0.001

VIII. Distances Between Fiducial Marks

Corner fiducials (diagonals)

1-2: 299.817 mm 3-4: 299.807 mm

Lines joining these markers intersect at an angle of 90° 00' 00"

Midside fiducials

5-6: 220.044 mm 7-8: 220.013 mm

Lines joining these markers intersect at an angle of 89° 59' 58"

Corner fiducials (perimeter)

1-3: 212.002 mm

1-4: 212.004 mm 2-4: 211.996 mm

The method of measuring these distances is considered accurate within 0.003 $\ensuremath{\text{mm}}$

2-3: 211.994 mm

Note: For GPS applications, the nominal entrance pupil distance from the focal plane is 282 mm.

