

- (00) measure the 9 control points described in the document under "Notes". measure each point on 2 images col01 and col02. Units must be pixels. For each measurement, estimate the uncertainty ($\frac{1}{2}, 1, 2, \dots, 5 \dots$ pixels). Before we use these ground coordinates will be provided.

Build a suite of matlab functions & a generic "main" program:

- (0) main program: read and store support data for 2 images. This includes ephemeris, attitude, & constants, times, etc. so that you can access them by an additional array index.

```
suggestion: ephdata = zeros(13, 1011, 2); % col01
temp = fscanf(... [13, 1011]);
ephdata(:, :, 1) = temp;
% next file col02
temp = fscanf(... [13, 969]);
ephdata(:, 1:969, 2) = temp;
```

If you prefer to do this with classes etc., ok. We just need to work with multiple images at the same time

make all of this support data global so it can be accessed by any function which also declares it as global. (* read 10 header lines)

- (1) function $\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \text{FI2G}(im\#, l, s, h, \Delta p)$ This implements

the image to ground projection done in HW1. The Δp vector will be:

$$\Delta p = \begin{bmatrix} \Delta g_i \\ \Delta g_j \\ \Delta g_k \\ \Delta g_s \\ \Delta X_s \\ \Delta Y_s \\ \Delta Z_s \end{bmatrix}$$

Note the nominal values for all elements of Δp are zero. If any are nonzero then you have changed the physical model (which we will do later)

for now $im\#$ will be either 1 or 2
 show that you get same result as HW1

(2) function $\begin{bmatrix} \phi \\ \lambda \end{bmatrix} = \text{FI2G_PL}(im\#, l, s, h, \Delta p)$ This is just a wrapper of FI2G (1) + a conversion from cartesian to geographic.

(3) function $\begin{bmatrix} \Delta \phi \\ \Delta \lambda \end{bmatrix} = \text{FI2G_PL-0}(im\#, l, s, h, \phi, \lambda, \Delta p)$
(Zero)

This is just a wrapper of FI2G-PL (2) + a subtraction. The output vector is just a misclosure between input ϕ, λ and the ϕ, λ produced from l, s, h . It is just

$$\begin{bmatrix} \Delta \phi \\ \Delta \lambda \end{bmatrix} = \begin{bmatrix} \phi \\ \lambda \end{bmatrix} - \text{FI2G_PL}(im\#, l, s, h, \Delta p)$$

(4) using function (3) FI2G-PL-0 we next numerically solve for l, s as unknowns, given input ϕ, λ, h . In other words, we invert FI2G-PL. make function $\begin{bmatrix} l \\ s \end{bmatrix} = \text{FG2I}(im\#, \phi, \lambda, h, \Delta p)$

to accomplish this.

(a) start with $(l^0, s^0) = (0, 0)$, input $\phi, \lambda, h, \Delta p$

(b) compute $\begin{bmatrix} F_\phi \\ F_\lambda \end{bmatrix} = \text{FI2G_PL-0}(im\#, l^0, s^0, h, \phi, \lambda, \Delta p)$

(c) compute partial derivatives $\frac{\partial F_\phi}{\partial l}, \frac{\partial F_\phi}{\partial s}, \frac{\partial F_\lambda}{\partial l}, \frac{\partial F_\lambda}{\partial s}$ numerically:

$$\begin{bmatrix} \frac{\partial F_\phi}{\partial l} \\ \frac{\partial F_\lambda}{\partial l} \end{bmatrix} \approx \frac{\text{FI2G_PL-0}(im\#, l^0 + \Delta l, s^0, h, \phi, \lambda, \Delta p) - \text{FI2G_PL-0}(im\#, l^0, s^0, h, \phi, \lambda, \Delta p)}{\Delta l}$$

$$\begin{bmatrix} \frac{\partial F_\phi}{\partial s} \\ \frac{\partial F_\lambda}{\partial s} \end{bmatrix} \approx \frac{\text{FI2G_PL-0}(im\#, l^0, s^0 + \Delta s, h, \phi, \lambda, \Delta p) - \text{FI2G_PL-0}(im\#, l^0, s^0, h, \phi, \lambda, \Delta p)}{\Delta s}$$

Iteration Loop

(d) solve newton iteration step for corrections to l^0, s^0 :

$$\begin{bmatrix} \frac{\partial F_\phi}{\partial l} & \frac{\partial F_\phi}{\partial s} \\ \frac{\partial F_\lambda}{\partial l} & \frac{\partial F_\lambda}{\partial s} \end{bmatrix} \begin{bmatrix} \Delta l \\ \Delta s \end{bmatrix} = \begin{bmatrix} -F_\phi \\ -F_\lambda \end{bmatrix}$$

note: $\Delta l, \Delta s$ in step (c) are perturbations to estimate partials. Here $\Delta l, \Delta s$ are corrections to refine current estimate l^0, s^0 .

$$J \Delta = -F$$

$$\Delta = -J^{-1} \cdot F$$

(e) update l^0, s^0

$$\begin{bmatrix} l_{new}^0 \\ s_{new}^0 \end{bmatrix} = \begin{bmatrix} l_{old}^0 + \Delta l \\ s_{old}^0 + \Delta s \end{bmatrix}$$

iterate until $\Delta l, \Delta s$ are very small

After you are done iterating, the refined l, s are consistent with ϕ, λ, h and you have solved the ground to image projection problem.

$$\begin{bmatrix} l \\ s \end{bmatrix} = FG2I(im\#, \phi, \lambda, h, \Delta p)$$

Note: equations in (d) are from Taylor Series Linearization

$$F_\phi(l, s) = 0, \quad F_\phi \approx F_\phi(l^0, s^0) + \frac{\partial F_\phi}{\partial l} \Delta l + \frac{\partial F_\phi}{\partial s} \Delta s = 0$$

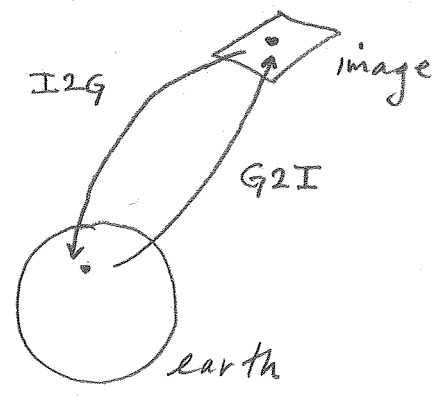
$$F_\lambda(l, s) = 0, \quad F_\lambda \approx F_\lambda(l^0, s^0) + \frac{\partial F_\lambda}{\partial l} \Delta l + \frac{\partial F_\lambda}{\partial s} \Delta s = 0$$



put this in matrix form and you get

$$J \Delta = -F$$

(★) verify function (4) by input any ϕ, λ, h in the image, compute l, s . Then use function (2) to verify that you get back ϕ, λ, h . What is the difference? You could do this with a control point, but any point works.



this should be a closed loop.

Apply Δp in the function F12G as follows:

- interpolate g_i, g_j, g_k, g_s based on line number and corresponding time
- unitize \vec{q}
- revise
 - $g_i = g_i + \Delta g_i$
 - $g_j = g_j + \Delta g_j$
 - $g_k = g_k + \Delta g_k$
 - $g_s = g_s + \Delta g_s$
- unitize \vec{q}
- interpolate X_s, Y_s, Z_s base on line number and corresponding time
- revise
 - $X_s = X_s + \Delta X_s$
 - $Y_s = Y_s + \Delta Y_s$
 - $Z_s = Z_s + \Delta Z_s$

recall $\vec{\Delta p} =$

Δg_i
Δg_j
Δg_k
Δg_s
ΔX_s
ΔY_s
ΔZ_s

Functions to compute partial derivatives:

(5) for function $\begin{bmatrix} \phi \\ \lambda \end{bmatrix} = \text{FI2G_PL}(im\#, l, s, h, \Delta p)$, make

$$\begin{bmatrix} \frac{\partial \phi}{\partial l} & \frac{\partial \phi}{\partial s} & \frac{\partial \phi}{\partial h} & \frac{\partial \phi}{\partial q_i} & \frac{\partial \phi}{\partial q_j} & \frac{\partial \phi}{\partial q_k} & \frac{\partial \phi}{\partial q_s} & \frac{\partial \phi}{\partial x_s} & \frac{\partial \phi}{\partial y_s} & \frac{\partial \phi}{\partial z_s} \\ \frac{\partial \lambda}{\partial l} & \frac{\partial \lambda}{\partial s} & \frac{\partial \lambda}{\partial h} & \frac{\partial \lambda}{\partial q_i} & \frac{\partial \lambda}{\partial q_j} & \frac{\partial \lambda}{\partial q_k} & \frac{\partial \lambda}{\partial q_s} & \frac{\partial \lambda}{\partial x_s} & \frac{\partial \lambda}{\partial y_s} & \frac{\partial \lambda}{\partial z_s} \end{bmatrix} = \text{FI2G_PL_PARTIALS}(im\#, l, s, h, \Delta p) \quad (5)$$

(6) for function $\begin{bmatrix} l \\ s \end{bmatrix} = \text{FG2I}(im\#, \phi, \lambda, h, \Delta p)$, make

$$\begin{bmatrix} \frac{\partial l}{\partial \phi} & \frac{\partial l}{\partial \lambda} & \frac{\partial l}{\partial h} & \frac{\partial l}{\partial q_i} & \frac{\partial l}{\partial q_j} & \frac{\partial l}{\partial q_k} & \frac{\partial l}{\partial q_s} & \frac{\partial l}{\partial x_s} & \frac{\partial l}{\partial y_s} & \frac{\partial l}{\partial z_s} \\ \frac{\partial s}{\partial \phi} & \frac{\partial s}{\partial \lambda} & \frac{\partial s}{\partial h} & \frac{\partial s}{\partial q_i} & \frac{\partial s}{\partial q_j} & \frac{\partial s}{\partial q_k} & \frac{\partial s}{\partial q_s} & \frac{\partial s}{\partial x_s} & \frac{\partial s}{\partial y_s} & \frac{\partial s}{\partial z_s} \end{bmatrix} = \text{FG2I_PARTIALS}(im\#, \phi, \lambda, h, \Delta p) \quad (6)$$

for partials let $\Delta q_{i,j,k,s} = 1 \times 10^{-6}$
 $\Delta x_s, y_s, z_s = 1 \times 10^{-4}$ (units meters)
 $\Delta \phi, \lambda = 1 \times 10^{-8}$ (units radians)
 $\Delta h = 1 \times 10^{-4}$ (units meters)

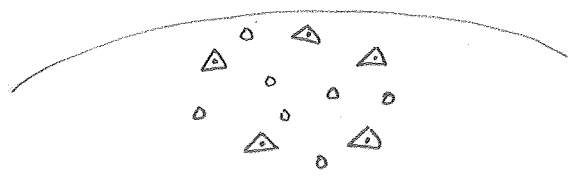
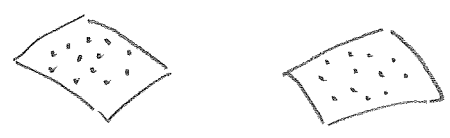
(7) $\begin{bmatrix} \Delta l \\ \Delta s \end{bmatrix} = \text{FG2I_ls_0}(im\#, \phi, \lambda, h, l, s, \Delta p)$ { like collinearity equations for frame photogrammetry }

$$\begin{bmatrix} \Delta l \\ \Delta s \end{bmatrix} = \begin{bmatrix} l \\ s \end{bmatrix} - \text{FG2I}(im\#, \phi, \lambda, h, \Delta p)$$

(8) partials of function (7)

$$\begin{bmatrix} \frac{\partial F_2}{\partial \phi} & \frac{\partial F_2}{\partial \lambda} & \frac{\partial F_2}{\partial h} & \frac{\partial F_2}{\partial q_i} & \frac{\partial F_2}{\partial q_j} & \frac{\partial F_2}{\partial q_k} & \frac{\partial F_2}{\partial q_s} & \frac{\partial F_2}{\partial x_s} & \frac{\partial F_2}{\partial y_s} & \frac{\partial F_2}{\partial z_s} \\ \frac{\partial F_3}{\partial \phi} & \frac{\partial F_3}{\partial \lambda} & \frac{\partial F_3}{\partial h} & \frac{\partial F_3}{\partial q_i} & \frac{\partial F_3}{\partial q_j} & \frac{\partial F_3}{\partial q_k} & \frac{\partial F_3}{\partial q_s} & \frac{\partial F_3}{\partial x_s} & \frac{\partial F_3}{\partial y_s} & \frac{\partial F_3}{\partial z_s} \end{bmatrix} = \text{FG2I_ls_0_PARTIALS}(im\#, \phi, \lambda, h, l, s, \Delta p) \quad (8)$$

In a bundle block adjustment the observations are l, s on the images, constants are ϕ, d, h for control points, plus any satellite parameters NOT adjusted, unknowns are ϕ, d, h of pass points (tie points) and Δp 's for any adjustable parameters on any images



\circ = pass point
 Δ = control point

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- hand in measurements (note we do not actually use them here !)
 - hand in source code for 8 functions
 - show result of function evaluated at control point of HW 4
 - show $\downarrow \uparrow$ closed loop for F12G-PL \in FG2I