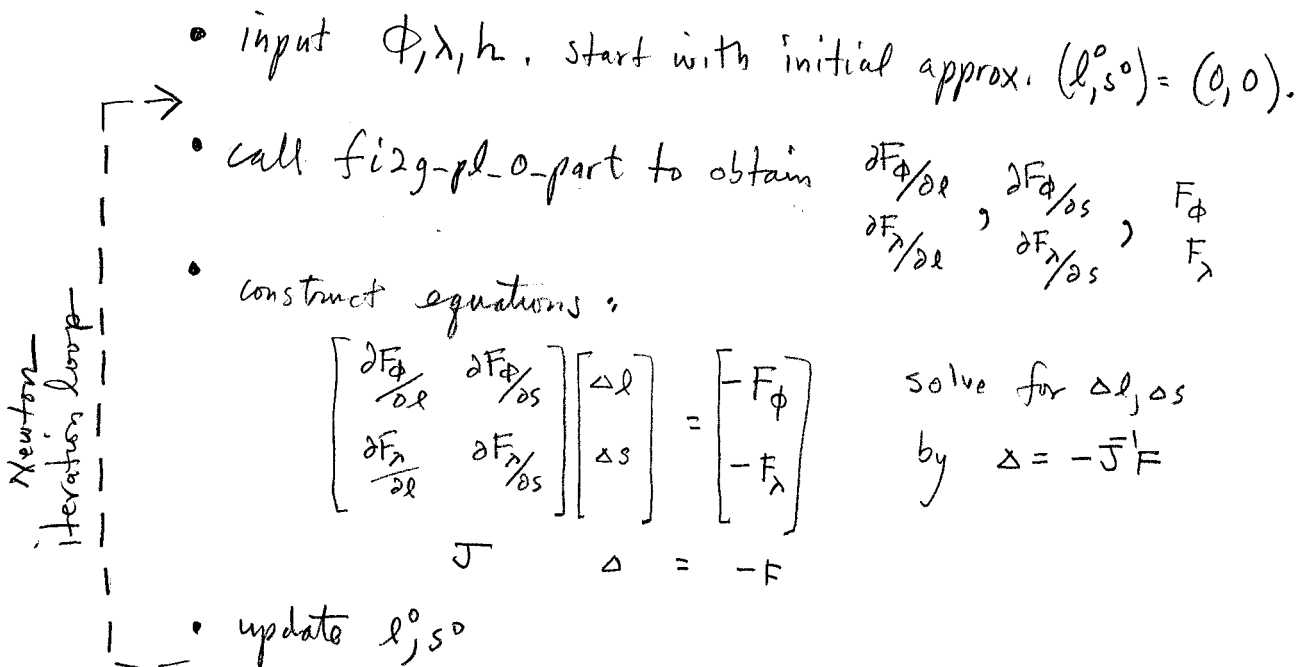


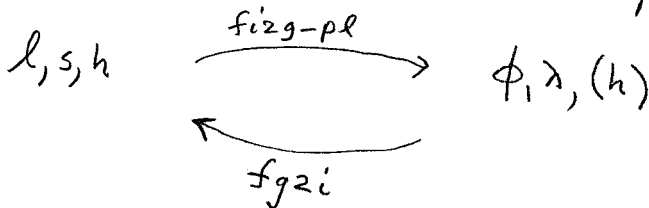
Orthorectification assigned 1 Mar. 2017, due 24 Mar. (Fri)

Create functions $\begin{bmatrix} l \\ s \end{bmatrix} = \text{fgzi}(\phi, \lambda, h, dp)$

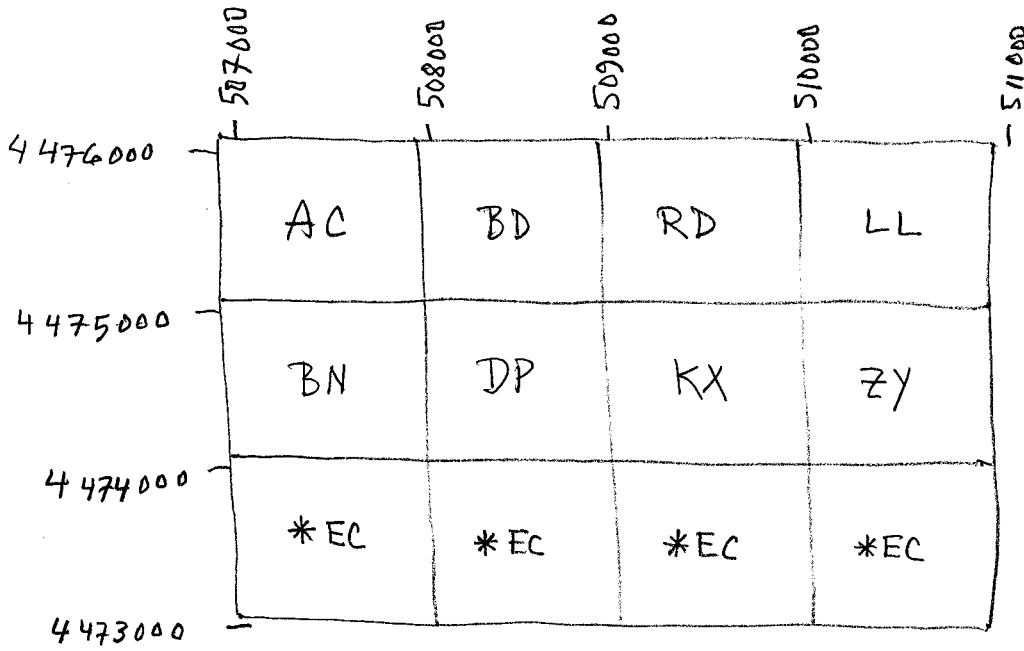
This will call `fizg-pl-0` but we switch the roles of knowns and unknowns. Now ϕ, λ, h are known and l, s are to be computed. Do by iterative inversion.

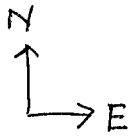


when it "works", verify numerically that it is inverse of `fizg-pl`:



Use the above created function fgz_i to make an ortho rectification of your assigned tile at 0.5m GSD in coordinate system ISP West, meters




 will be
 seamless mosaic
 no overlap between
 tiles.

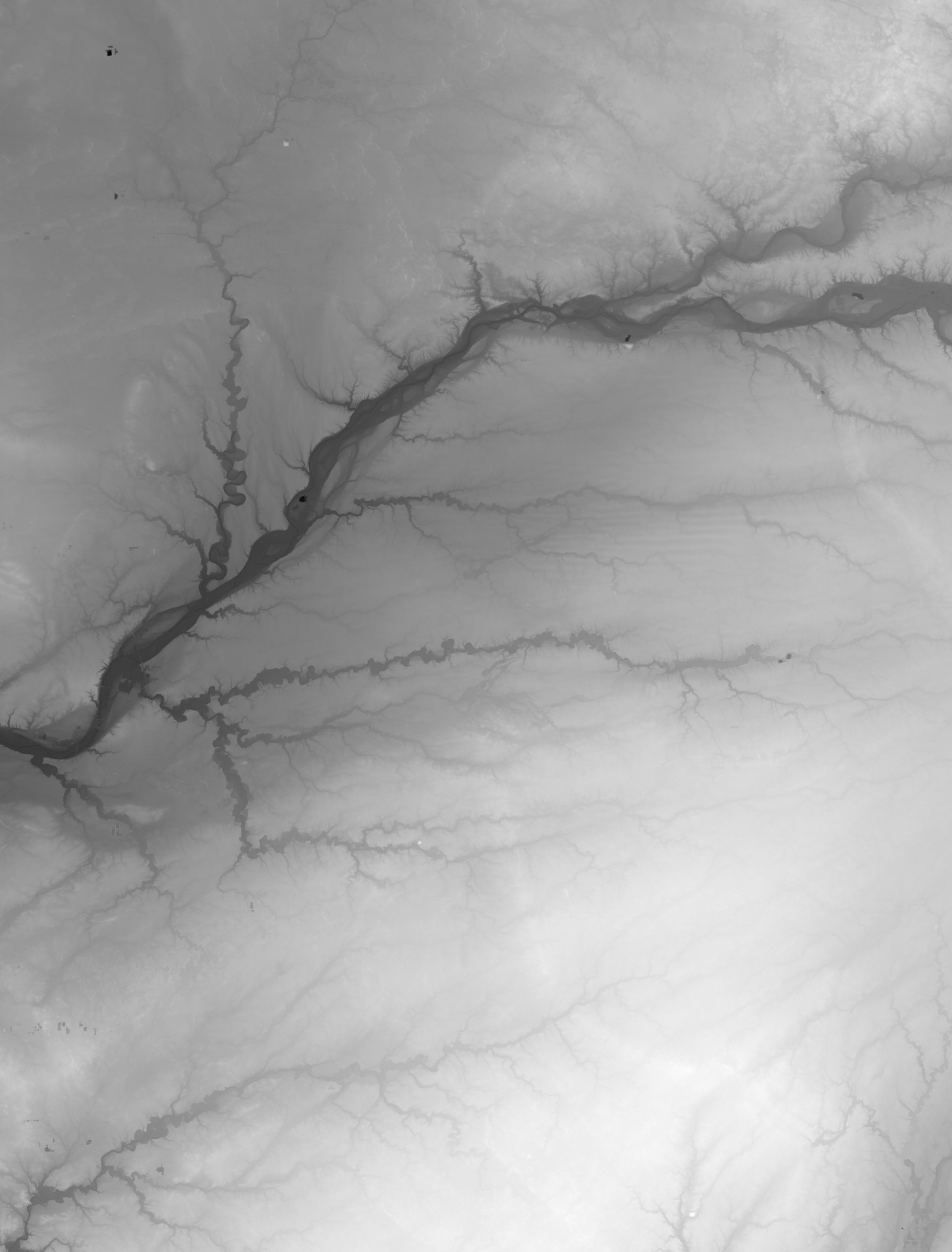
each tile is 1000 x 1000 m or 2000 x 2000 pixels

you may use `ftmgeo-utmz16.m` on ftp folder.

$$\begin{bmatrix} \phi \\ \lambda \end{bmatrix} = \text{ftmgeo_utmz16}(E, N)$$

(radians) (meters)

more instructions coming on DEM, N, image structure, world file format, ESRI vector overlay, ...



reading in the DEM data:

```
fid = fopen('usgs.flt', 'r');
temp = fread(fid, [3612, 3612], 'single');
dem = temp'; % transpose
clear temp
```

Do this only once!
at the beginning of program

interpolate height at ϕ, λ

$$r_2 = \text{fix}[(\phi_T - \phi) / \Delta\phi] + 1$$

$$r_1 = r_2 + 1$$

$$c_1 = \text{fix}[(\lambda - \lambda_L) / \Delta\lambda] + 1$$

$$c_2 = c_1 + 1$$

$$\phi_1 = \phi_T - (r_1 - 1) * \Delta\phi$$

$$\phi_2 = \phi_1 + \Delta\phi$$

$$\lambda_1 = \lambda_L + (c_1 - 1) * \Delta\lambda$$

$$\lambda_2 = \lambda_1 + \Delta\lambda$$

$$\text{frac-}\phi = (\phi - \phi_1) / \Delta\phi$$

$$\text{frac-}\lambda = (\lambda - \lambda_1) / \Delta\lambda$$

$$x = \text{frac-}\lambda$$

$$y = \text{frac-}\phi$$

$$g_1 = \text{dem}(r_1, c_1)$$

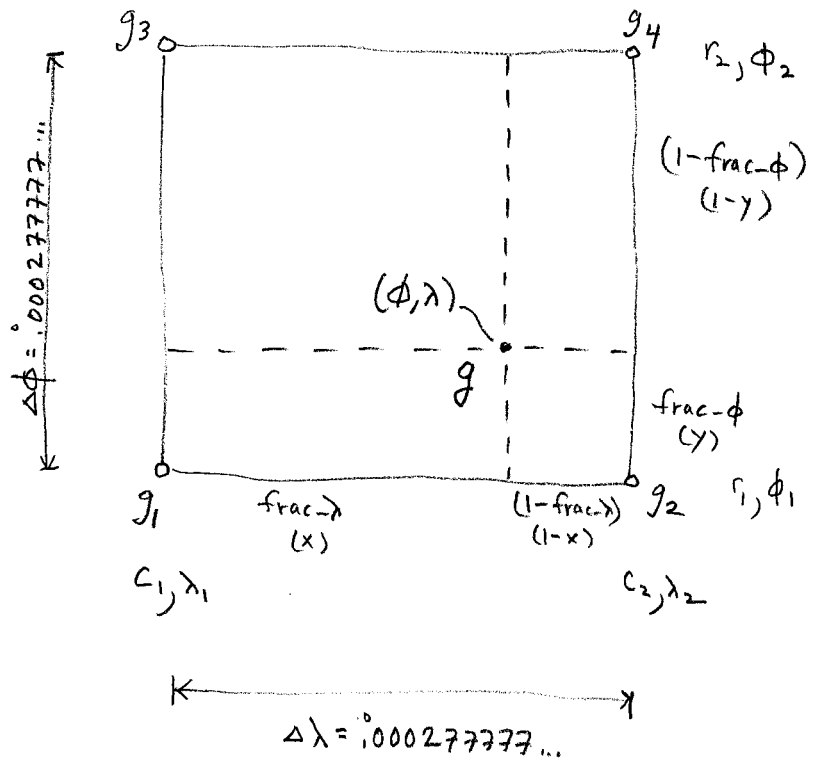
$$g_2 = \text{dem}(r_1, c_2)$$

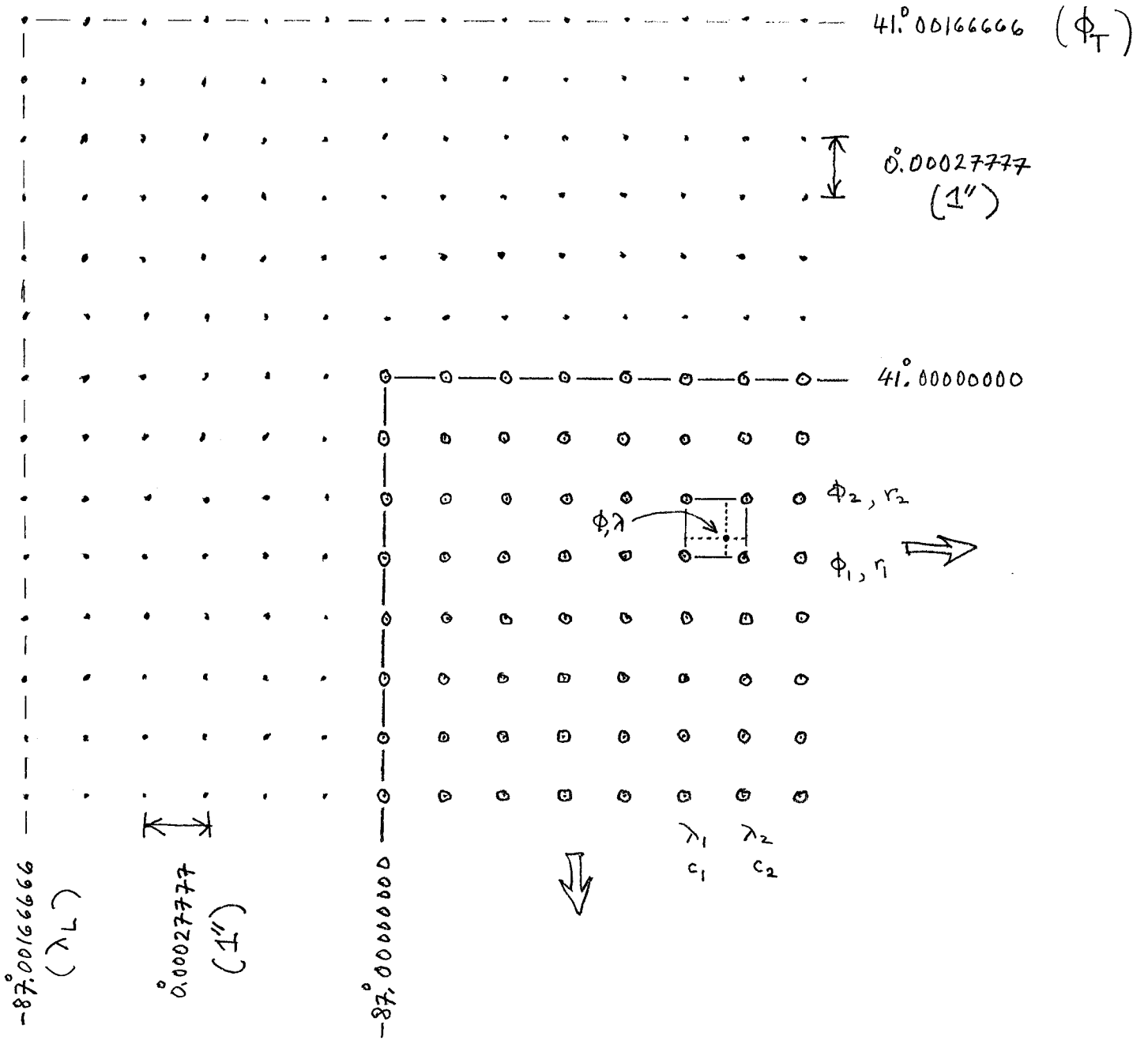
$$g_3 = \text{dem}(r_2, c_1)$$

$$g_4 = \text{dem}(r_2, c_2)$$

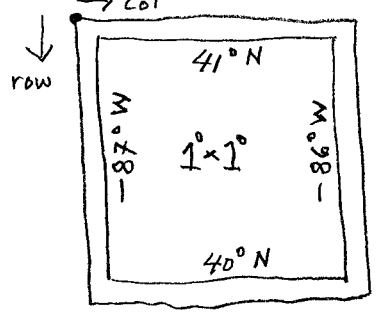
$$g = (1 - x - y + xy) * g_1 + (x - xy) * g_2 + (y - xy) * g_3 + (xy) * g_4$$

g is the orthometric (sea level) height at location ϕ, λ usually denoted as H .





6 extra rows/columns on N, S, E, W edges
 → col



1st row is at the top (N)
 elements in row proceed
 L → R (W → E)

need index arithmetic to interpolate
 height at ϕ, λ from the grid

USGS 1 arc second DEM
 "grid float" format

geoid12b_laf.txt

40 27 00	-33.68	-33.70	-33.72	-33.75	-33.78
40 26 00	-33.67	-33.69	-33.71	-33.74	-33.76
40 25 00	-33.66	-33.68	-33.70	-33.72	-33.74
40 24 00	-33.64	-33.66	-33.68	-33.71	-33.73
	00	00	00	00	00
	56	55	54	53	52
	-86	-86	-86	-86	-86

load geoid12b_laf.txt

$$\Delta\phi = 1 \text{ min} = \frac{1}{60} \text{ deg} = .01666\dots$$

$$\Delta\lambda = 1 \text{ min} = \frac{1}{60} \text{ deg} = .01666\dots$$

$$\phi_B = 40.4, \quad \lambda_L = -86.9333\dots$$

interpolate N at $\phi, \lambda =$

$$r_1 = \text{fix} \left[(\phi - \phi_B) / \Delta\phi \right] + 1$$

$$r_2 = r_1 + 1$$

$$c_1 = \text{fix} \left[(\lambda - \lambda_L) / \Delta\lambda \right] + 1$$

$$c_2 = c_1 + 1$$

$$\phi_1 = \phi_B + (r_1 - 1) * \Delta\phi$$

$$\lambda_1 = \lambda_L + (c_1 - 1) * \Delta\lambda$$

$$\text{frac-}\phi = (\phi - \phi_1) / \Delta\phi$$

$$\text{frac-}\lambda = (\lambda - \lambda_1) / \Delta\lambda$$

$$x = \text{frac-}\lambda$$

$$y = \text{frac-}\phi$$

$$g_1 = \text{geoid12b-laf}(r_1, c_1)$$

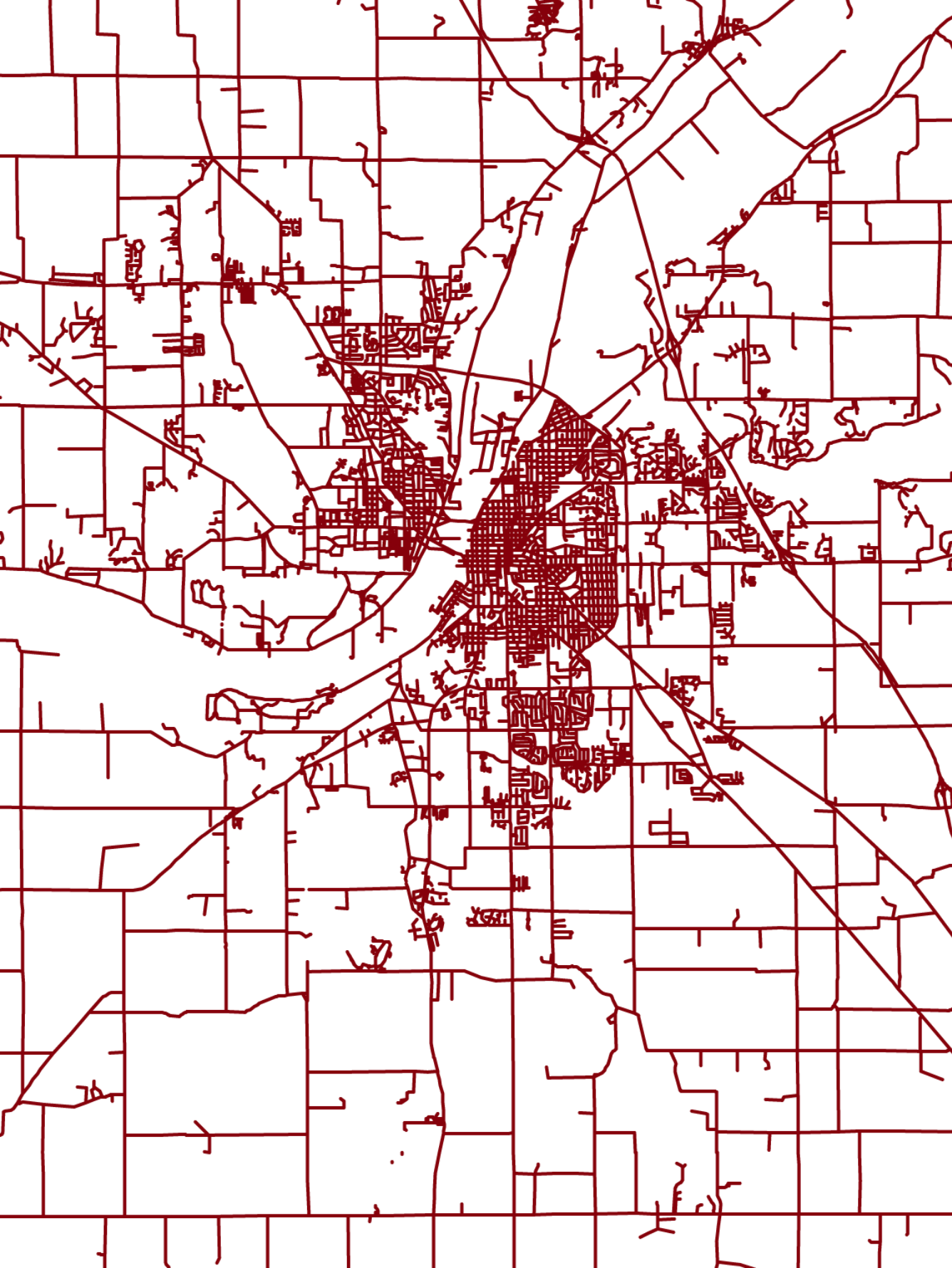
$$g_2 = \text{geoid12b-laf}(r_1, c_2)$$

$$g_3 = \text{geoid12b-laf}(r_2, c_1)$$

$$g_4 = \text{geoid12b-laf}(r_2, c_2)$$

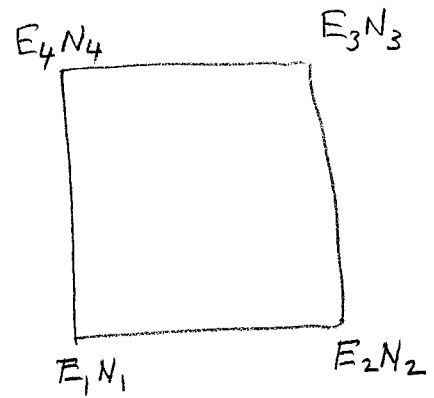
$$g = (1 - x - y + x * y) * g_1 + (x - x * y) * g_2 + (y - x * y) * g_3 + (x * y) * g_4$$

$$N = g$$



vector overlay to check geometry

create a clipping rectangle for your tile (in matlab):



```
Bdry.Geometry = 'Polygon';
```

```
Bdry.X = [E1 E2 E3 E4 E1 NaN];
```

```
Bdry.Y = [N1 N2 N3 N4 N1 NaN];
```

```
Bdry.Name = 'Lafayette Ortho';
```

```
Bdry.BoundingBox = [min(Bdry.X) min(Bdry.Y) ; max(Bdry.X) max(Bdry.Y)];
```

```
% = [E1 N1 ; E2 N3]
```

```
Shapewrite(Bdry, 'boundary');
```


% This will write boundary.shp, .shx, .dbf

% you can use this to clip the vector data to only your image tile

to clip (crop) vector data :

Start ArcMap

- blank map

- connect to folder  (catalog tab)

- add data

 - road_2


 - boundary (from above!)

- geoprocessing

 - clip

 - clip dialogue

 - input feature
 - clip feature
 - output feature
 - xy tolerance 0.5

 - 

template/flowchart for orthorectification code

```

in_img = imread('laf01.tif', 'TIFF');
[nrows, ncols] = size(in_img);
out_img = zeros(nrows, ncols, 'uint8');
for i = 1:nrows

```

```

    for j = 1:ncols

```

$$E = E_{min} + (j-1) * GSD ;$$

$$N = N_{max} - (i-1) * GSD ;$$

Transform $E, N \rightarrow \Phi, \lambda$

Interpolate H from DEM

Interpolate N from geoid grid

$$h = N + H ;$$

$$\begin{bmatrix} l \\ s \end{bmatrix} = fg2i(\Phi, \lambda, h, dp)$$

if l, s both in range ($> 2, < \text{max}-1$)

$$g = \text{interpolate intensity from in_img} \% 0 - 255$$

else

$$g = 128$$

end

$$\text{out_img}(i, j) = \text{uint8}(\text{round}(g))$$

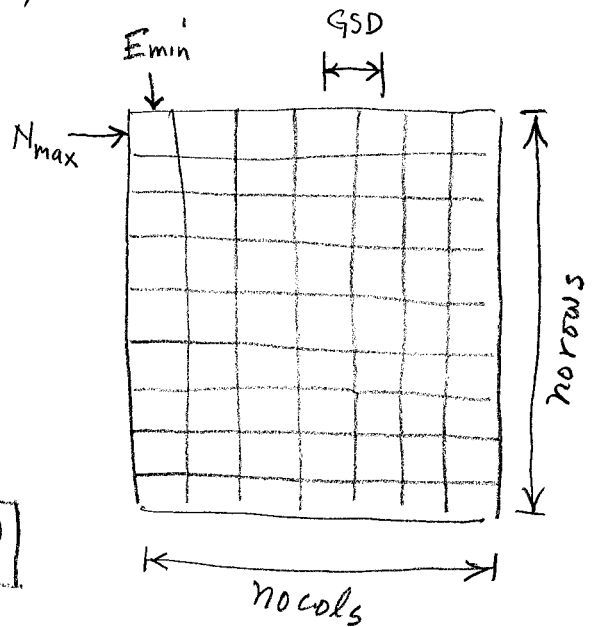
end % j-loop

end % i-loop

```

imwrite(out_img, 'outfile.jpg', 'JPEG');

```



Esri "world file"

□.tif → □.tfw

□.jpg → □.jgw



text file with 6 numbers, create with notepad, etc.

```
GSD X
0
0
- GSD Y
X upper left
Y upper left
```

note: intensity from image is uint8, convert to double before doing math
 $gd = \text{double}(g)$; etc.

Turn in:

1. code (hard copy & email, incl. all functions)
 2. hardcopy maps, image + overlay, arrange brightness/contrast and color so visible
 3. Zoom in to show registration in a "few" places... good, bad, consistent, hypotheses?
 4. □.jpg, □.jgw
- ± will merge all submissions into a mosaic